



Universidad de Jaén

Departamento de Informática



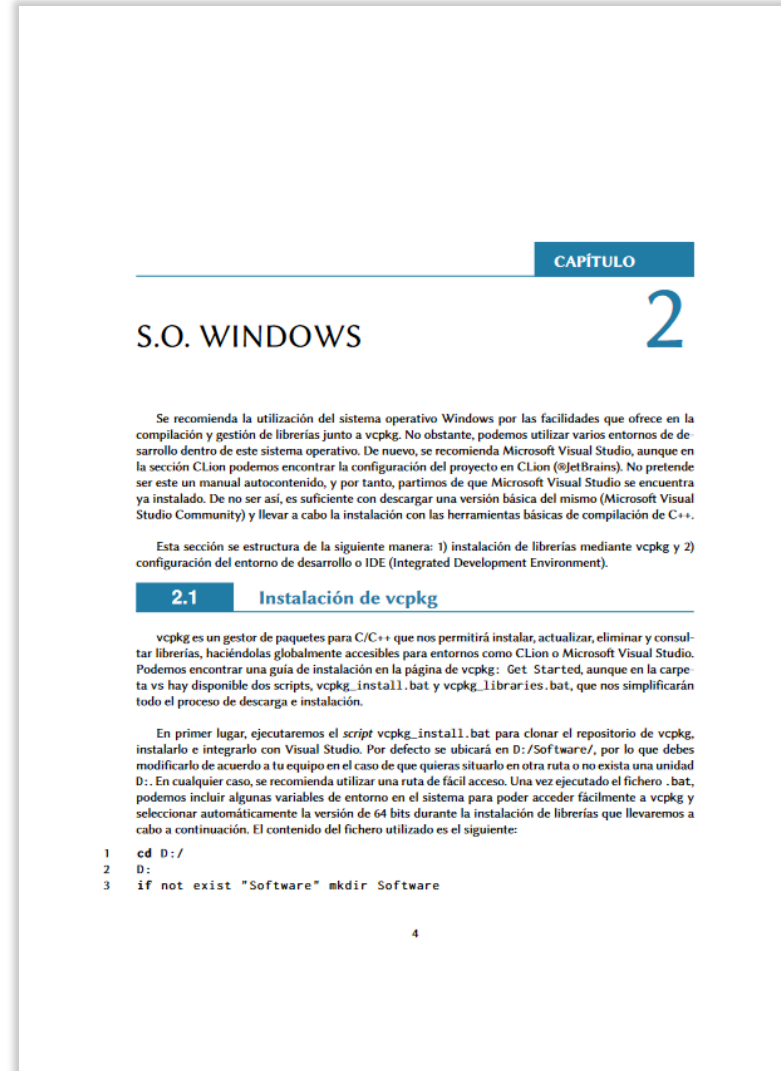
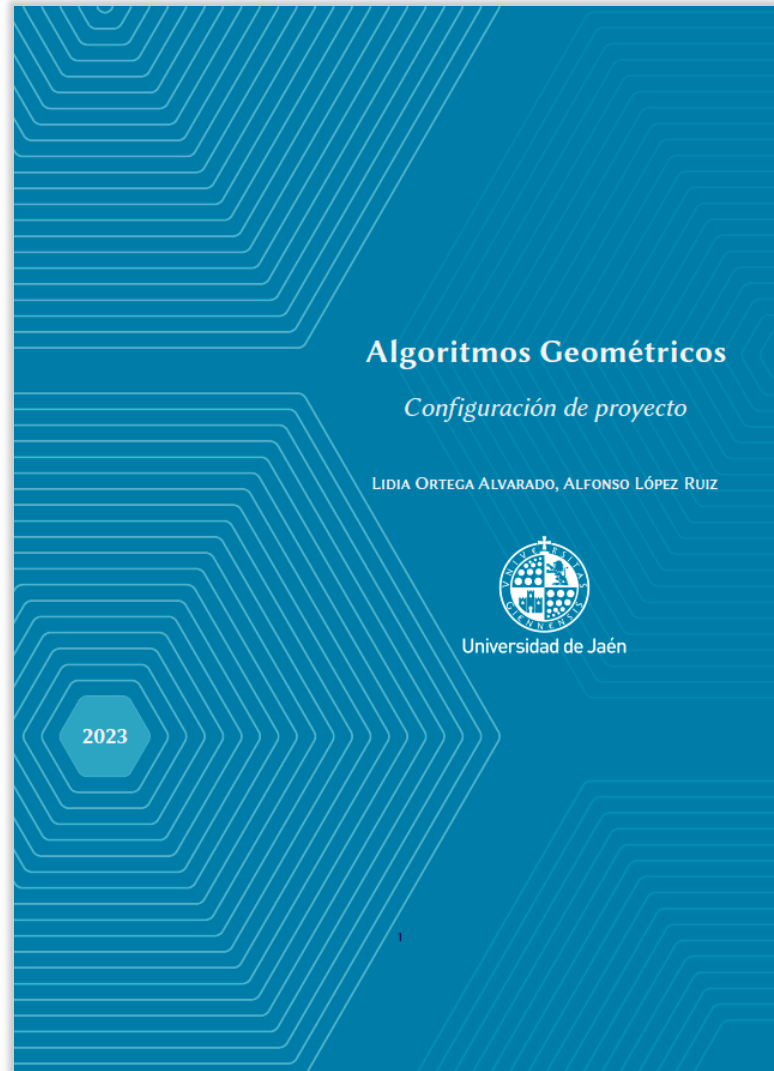
Práctica 1 Algoritmos geométricos

Grado en Ingeniería Informática

Alfonso López Ruiz

Curso 2022-2023

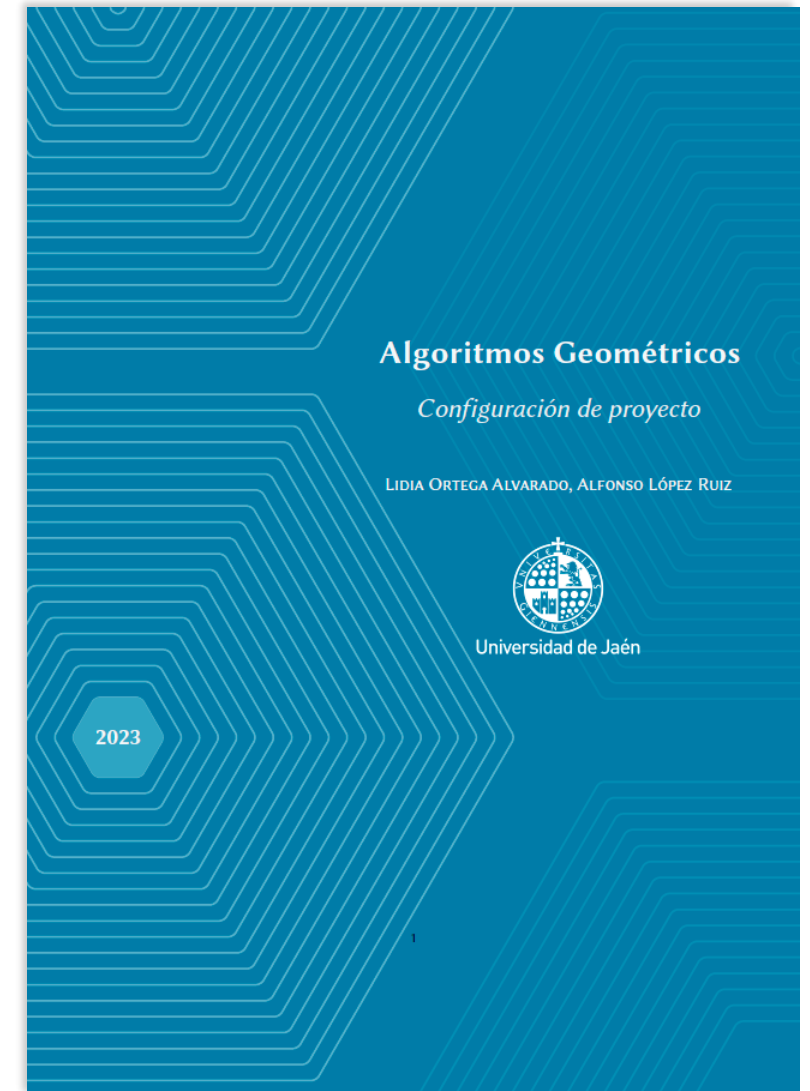
- **Starting point:** a C++ project with OpenGL as the baseline renderer.



Installation Guide

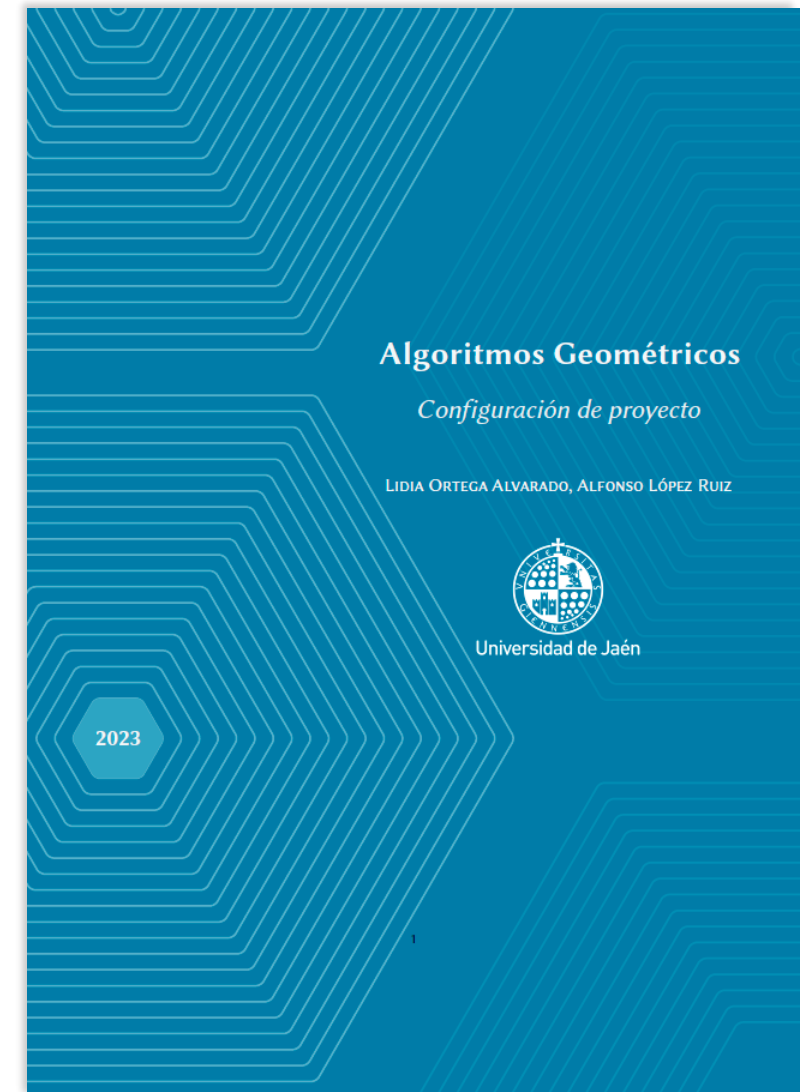
3

- ▶ **Starting point:** a C++ project with OpenGL as the baseline renderer.
 - ▶ Read carefully the installation guide uploaded to Platea.
 - ▶ Windows + Microsoft Visual Studio + vcpkg
 - ▶ Windows + JetBrains Clion + vcpkg
 - ▶ Linux + JetBrains CLion



Installation Guide

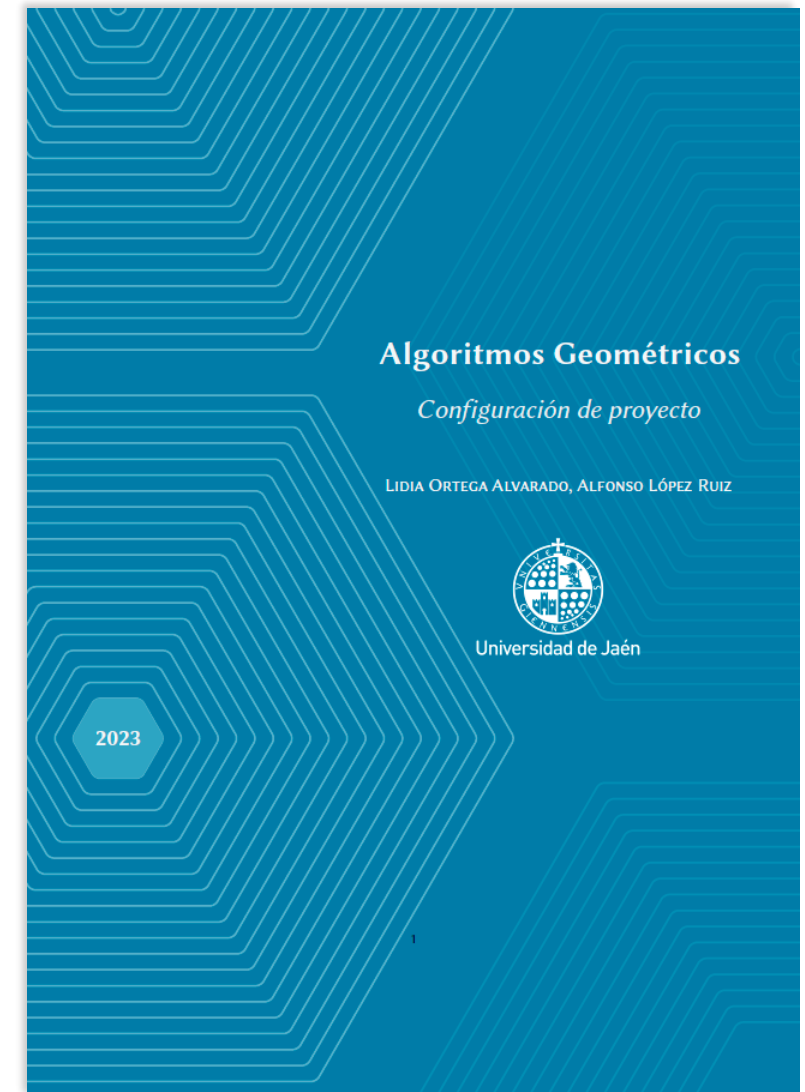
- ▶ **Starting point:** a C++ project with OpenGL as the baseline renderer.
 - ▶ It is recommended to use **vcpkg** since it facilitates the installation of libraries.
 - ▶ The installation flow is already prepared in **vcpkg_install.bat**.
 - ▶ The first step is to move to a folder, D:/Software.
 - ▶ Choose one of your choice in the script, if necessary.
 - ▶ Download git repository and install it.
 - ▶ Append vcpkg to the **environment variables** (this is not included in the provided .bat files).
 - ▶ Follow the guide instructions.
 - ▶ Libraries to be installed are also prepared in **vcpkg_libraries.bat**.
- ▶ Otherwise follow the vcpkg installation guide provided in their page.



Installation Guide

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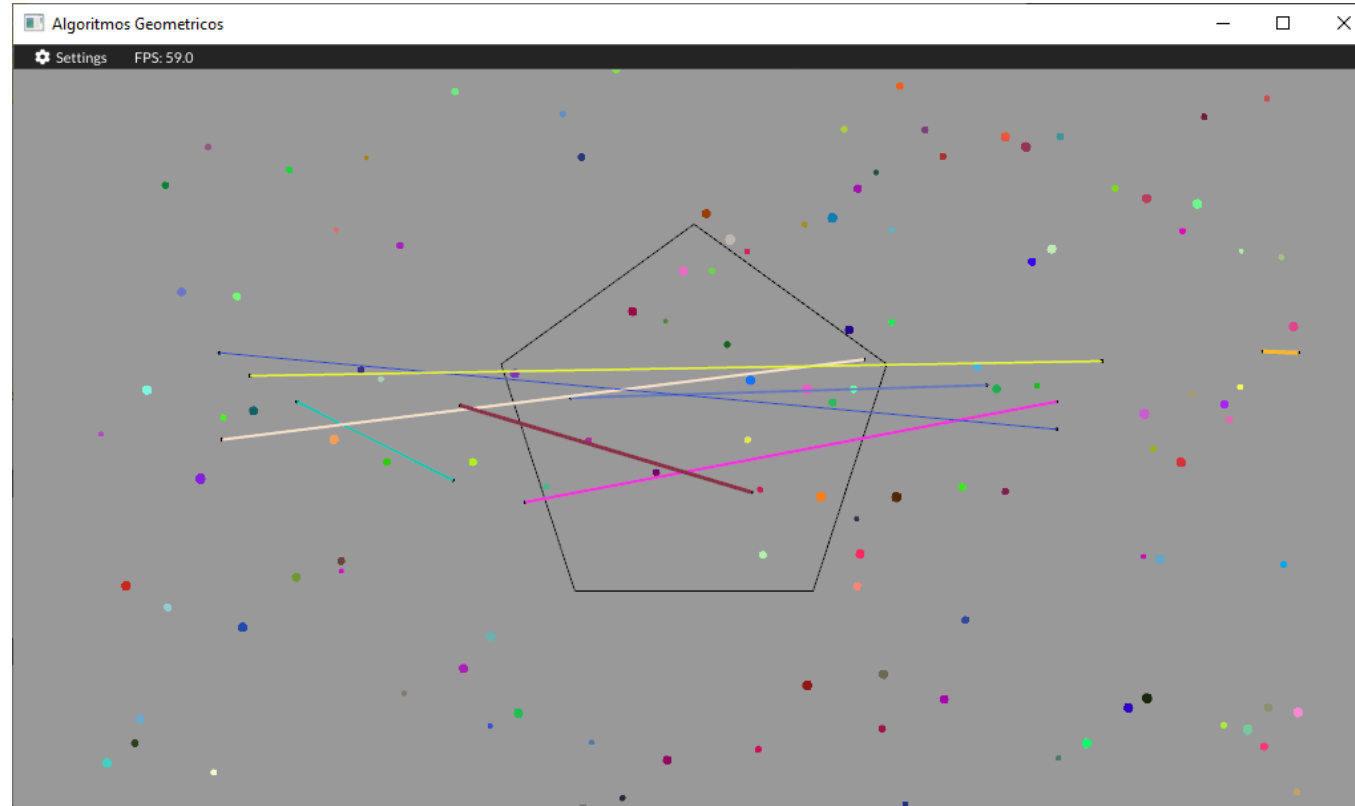
- ▶ **Starting point:** a C++ project with OpenGL as the baseline renderer.
 - ▶ If Microsoft Visual Studio was opened during vcpkg installation, please close it and reopen.
 - ▶ Once ready, the project should compile with no errors.
 - ▶ The first launch should fail as there are some missing .dll files.
 - ▶ The project needs the .dll files from the installed libraries.
 - ▶ Select **x64** as the target architecture in Visual Studio.
 - ▶ The necessary .dll files have been attached to the uploaded project under a **dll folder**, following the Debug and Release structure of Visual Studio.
 - ▶ Copy both Debug and Release to x64 folder, created by Microsoft Visual Studio after the first launch.



Installation Guide

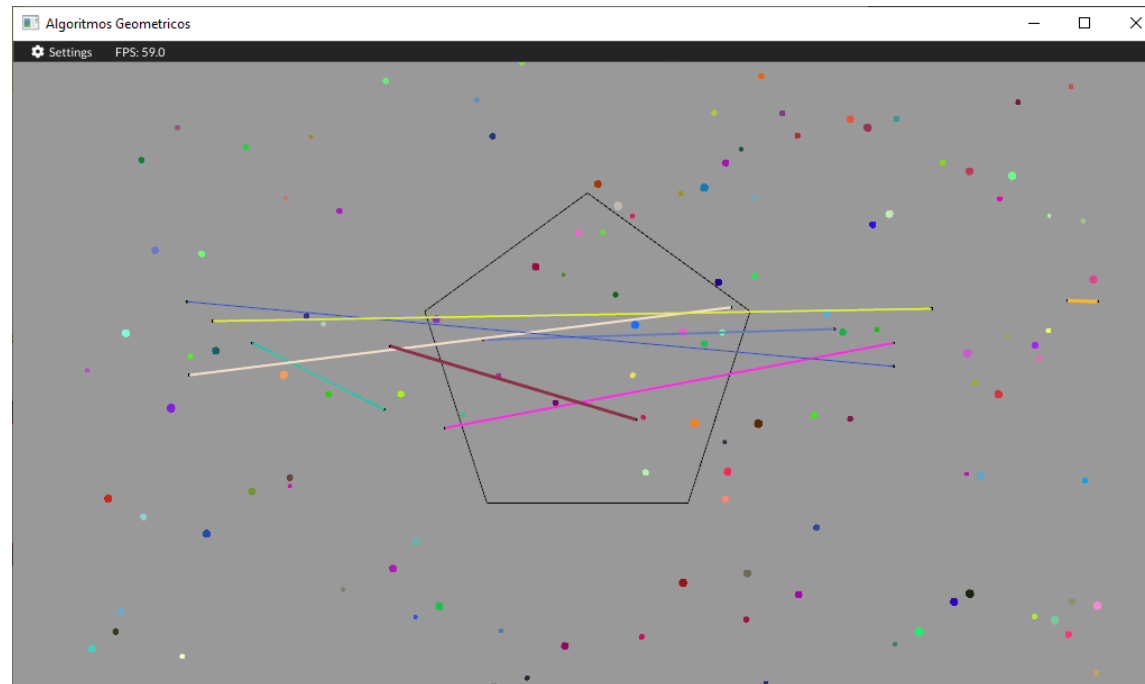
► **Starting point:** a C++ project with OpenGL as the baseline renderer.

- Everything should be up and running at this point.
- Something like the following image should be first rendered.



Installation Guide

- ▶ **Starting point:** a C++ project with OpenGL as the baseline renderer.
 - ▶ The camera has been limited to 2D for the first practices.
 - ▶ If the interaction feels a bit weird in 2D, just change the camera initialization and pass false instead of true to enable 3D.
 - ▶ You will have to in later practices.
 - ▶ The camera interaction is described in the installation guide. It is implemented to be Unity-like (more or less).



- ▶ **Starting point:** a C++ project with OpenGL as the baseline renderer.
 - ▶ Do not change code in graphics-related files.
 - ▶ It is intended to work on any mesh, primitive and shape to be implemented.
 - ▶ Files that must be modified:
 - ▶ **SceneContent:** includes the models and cameras that will be initialized by default.
 - ▶ Its only purpose is to isolate the creation of models and cameras from Renderer.
 - ▶ **Draw*:** these files are part of the objectives of this practice and the following.
 - ▶ Any file under the **Geometry** folder (or the ones that you will create, related to geometric shapes).

Practice 1

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
- ▶ Check everything is done before uploading the result.
- ▶ **Point:**
 - ▶ Constructor based on polar coordinates.
 - ▶ `getAlpha()`
 - ▶ `distance(p)`
 - ▶ `triangleArea(a, b)`
 - ▶ `classify(p0, p1)`
 - ▶ `slope(p)`

Practice 1

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- ▶ **Vect2D:**
 - ▶ Override `+`, `-`, `dot` and `scalar product` of a vector with respect to another vector.
 - ▶ Renderer of a vector.
 - ▶ It is just defined by a slope. We can draw it as a segment centred at $(0, 0)$ with its corresponding slope.

Practice 1

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
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- ▶ **SegmentLine:**
 - ▶ `isHorizontal()`
 - ▶ `isVertical()`
 - ▶ `getPoint(t)`
 - ▶ `getC()`
 - ▶ `segmentIntersection(s)`
 - ▶ `impSegmentIntersection(s)`

Practice 1

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- ▶ **Line:**
 - ▶ An infinite line.
 - ▶ Trick the user perception by using very large origin and destination points.
 - ▶ E.g., $(-1000, -1000, -1000) \rightarrow (1000, 1000, 1000)$.

Practice 1

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
- ▶ Check everything is done before uploading the result.
- ▶ **RayLine:**
 - ▶ Line clamped by origin, though it is infinite from this point.
 - ▶ Again, use large coordinates for the target point.

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
- ▶ Check everything is done before uploading the result.

- ▶ **Polygon:**
 - ▶ Implement constructor and storage methods with a common file format so they can interpret it properly.
 - ▶ E.g., CSV-like format, with each point in a new line, and each line composed of x, y (insert jump line).
 - ▶ Other solution which is easier to read, and a bit harder to implement: save the polygon points in a binary file.
 - ▶ `convex()`
 - ▶ `pointInConvexPolygon()`

Practice 1

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
- ▶ Check everything is done before uploading the result.

- ▶ **Vertex (from a polygon):**
 - ▶ `convex()`, `concave()`
 - ▶ `next()`, `previous()`
 - ▶ `nextEdge()`, `previousEdge()`

Practice 1

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
- ▶ Check everything is done before uploading the result.

- ▶ **Point cloud:**
 - ▶ Constructors and storage methods.
 - ▶ Use the file **RandomUtilities** for randomized point cloud.
 - ▶ `centralPoint()`
 - ▶ Renderer.

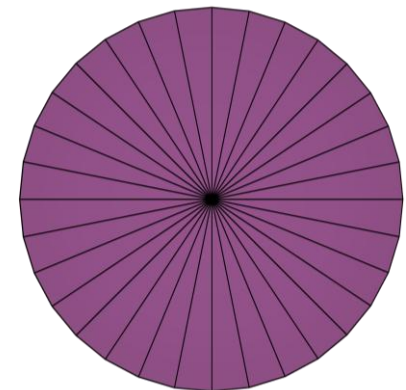
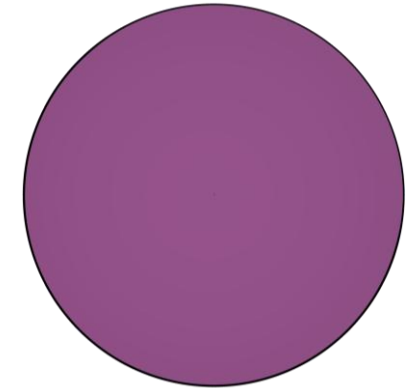
Practice 1

- ▶ **Objective:** to practice some of the 2D-based operations that were explained in theory lectures.
- ▶ Please, read carefully what ought to be implemented in this practice.
- ▶ Check everything is done before uploading the result.
- ▶ **Circle:**
 - ▶ `isInside(p)`

Practice 1

- **Final scenario:** you will have to compose a final scenario in **SceneContent**, consisting of previously implemented primitives.
1. **Random point cloud (100 points) + storage.**
 - Place it in a visible area within the viewport.
 2. **Three random segments using the cloud points.**
 3. **Select the points with minimum and maximum X and Y coordinates and create a polygon defined in counterclockwise direction.**
 - Check if its convex.
 4. **Draw 3 circumferences whose centre is the cloud point which is the closest to (0, 0). Pick a random point for each circumference and make it pass over the selected point (use it to calculate the radius).**

Preferred format for rendering a circumference.



Easier, uglier, but it is also ok.

▶ What should be uploaded?

- ▶ The whole project. Reduce the size with **Compile > Clean solution**.
- ▶ The executable file located either under **x64/Debug** or **x64/Release**.
 - ▶ Check it works before uploading. The Assets folder should be copied under x64/Debug or x64/Release so that the program can find these files.

▶ **Deadline:** February 13th, 23:59

How to implement a new rendering class

► You can find detailed instructions in the final chapter of the **uploaded guide**.

1. **Everything should be defined within the class constructor:** geometry and topology.
2. **Revise the concepts of geometry and topology.**
3. **Every model can be composed of several components.**
 - For instance, a point cloud could have two components: the point cloud itself and the convex hull calculated from it.
4. **Two vectors for each component:** geometry and topology.

How to implement a new rendering class

► Geometry and topology.

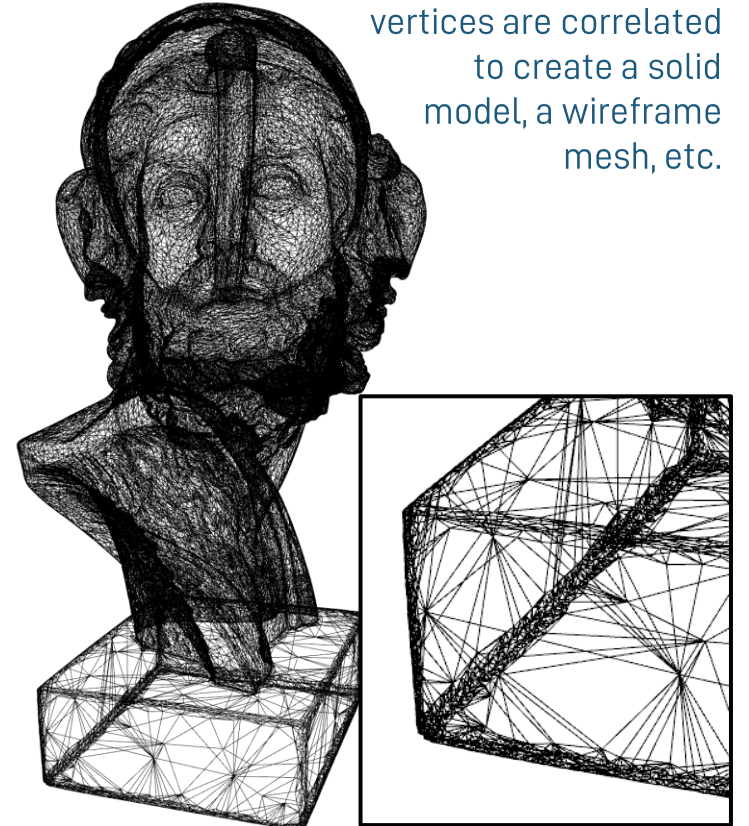
- Topology is called 'primitives' in your installation guide to avoid overlapping with later concepts.



Geometry: raw vertices.



Topology: defines how vertices are correlated to create a solid model, a wireframe mesh, etc.





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Práctica 4.B

Algoritmos geométricos

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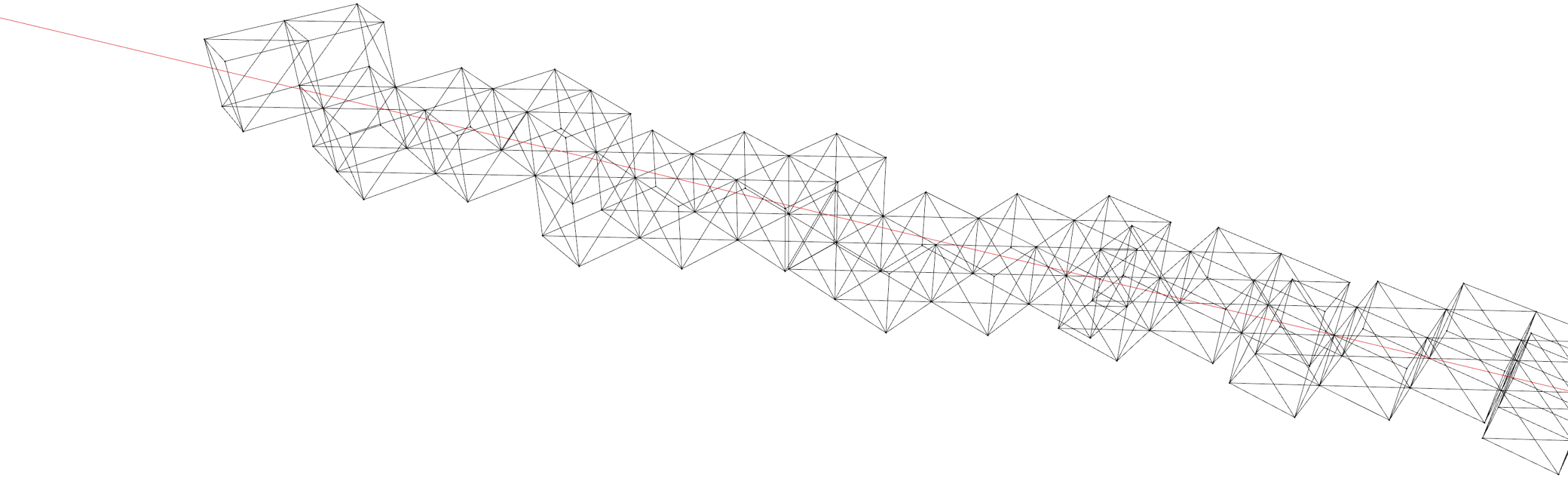
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A fast voxel traversal algorithm for ray tracing

► Lanzamos un rayo y obtenemos qué vóxeles atraviesa.

► Obtener dicho conjunto de vóxeles y renderizarlo:

► `new DrawVoxelization(voxels.data(), voxels.size(), voxels[0].extent() * 2.0f)`



A fast voxel traversal algorithm for ray tracing

► Lanzamos un rayo y obtenemos qué vóxeles atraviesa.

► Obtener dicho conjunto de vóxeles y renderizarlo:

► `new DrawVoxelization(voxels.data(), voxels.size(), voxels[0].extent() * 2.0f)`

► Los vóxeles grises pueden almacenar un conjunto de triángulos (opcional).

► Ejecutar test ray-triángulo en dichas primitivas.

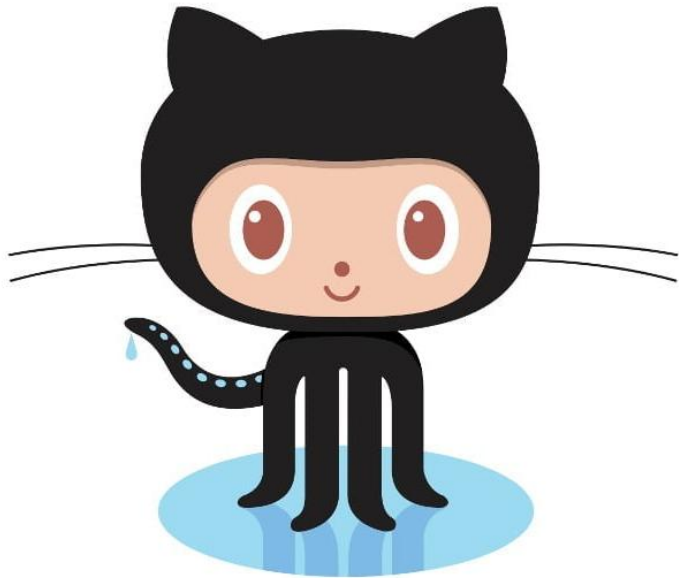
► Determinar qué primitivas son intersectadas y renderizarlas.

► **DrawTriangle**

A fast voxel traversal algorithm for ray tracing

► Algoritmo:

cgyurgyik/fast-voxel-traversal-algorithm



```
108     size_t current_Z_index = MAX(1, std::ceil(ray_start.z() - grid.minBound().z() / grid.voxelSizeZ()));
109     const size_t end_Z_index = MAX(1, std::ceil(ray_end.z() - grid.minBound().z() / grid.voxelSizeZ()));
110     int stepZ;
111     value_type tDeltaZ;
112     value_type tMaxZ;
113     if (ray.direction().z() > 0.0) {
114         stepZ = 1;
115         tDeltaZ = grid.voxelSizeZ() / ray.direction().z();
116         tMaxZ = tMin + (grid.minBound().z() + current_Z_index * grid.voxelSizeZ()
117             - ray_start.z()) / ray.direction().z();
118     } else if (ray.direction().z() < 0.0) {
119         stepZ = -1;
120         tDeltaZ = grid.voxelSizeZ() / -ray.direction().z();
121         const size_t previous_Z_index = current_Z_index - 1;
122         tMaxZ = tMin + (grid.minBound().z() + previous_Z_index * grid.voxelSizeZ()
123             - ray_start.z()) / ray.direction().z();
124     } else {
125         stepZ = 0;
126         tDeltaZ = tMax;
127         tMaxZ = tMax;
128     }
129
130     while (current_X_index != end_X_index || current_Y_index != end_Y_index || current_Z_index != end_Z_index) {
131         if (tMaxX < tMaxY && tMaxX < tMaxZ) {
132             // X-axis traversal.
133             current_X_index += stepX;
134             tMaxX += tDeltaX;
135         } else if (tMaxY < tMaxZ) {
136             // Y-axis traversal.
137             current_Y_index += stepY;
138             tMaxY += tDeltaY;
139         } else {
140             // Z-axis traversal.
141             current_Z_index += stepZ;
142             tMaxZ += tDeltaZ;
143         }
144     }
145 }
```

A fast voxel traversal algorithm for ray tracing

► Algoritmo:

- 1 ► Comprobar que el punto está dentro de la voxelización.
 - `glm::all(glm::greaterThanEqual(point, 0)) && ...`

A fast voxel traversal algorithm for ray tracing

► Algoritmo:

2

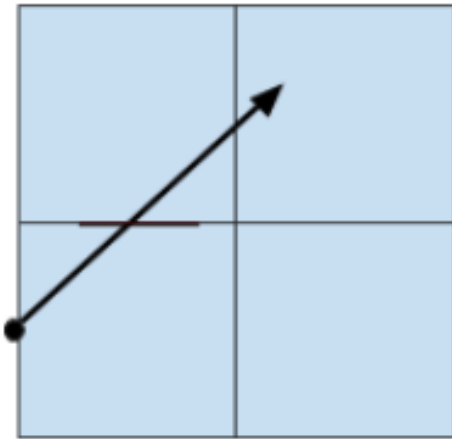
► Obtener avance en vóxel.

- Si el rayo tiene una coordenada x positiva, siempre avanzaremos +1 en X cuando sea necesario.
- Si el rayo tiene una coordenada x negativa, siempre avanzaremos -1 en X cuando sea necesario.
- `glm::sign(rayDirection)`

A fast voxel traversal algorithm for ray tracing

► Algoritmo:

- 3 ► Obtener la longitud del avance, $tDelta$.
 - $tDelta$ dependerá del tamaño de vóxel y de la dirección del rayo.
 - Nótese que se trata de un valor positivo siempre (es un t a lo largo del rayo).



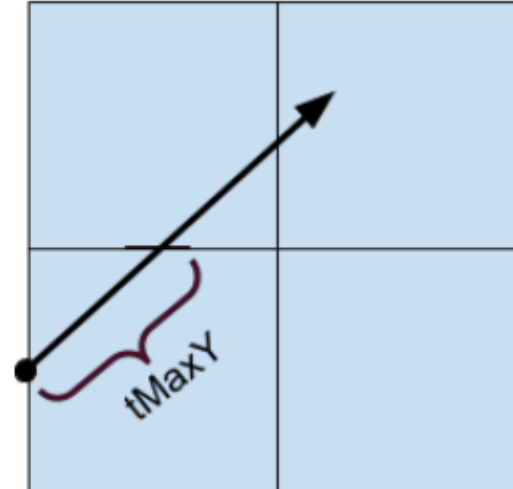
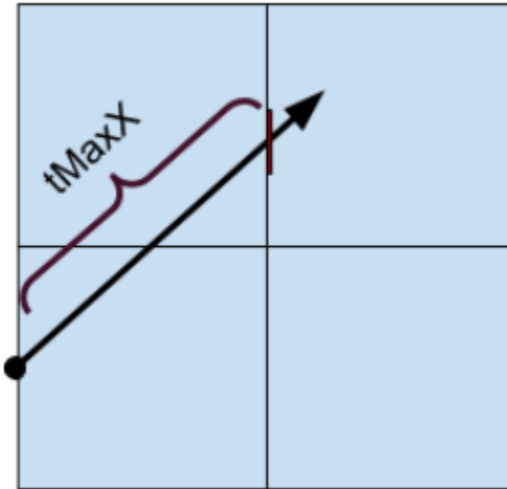
A fast voxel traversal algorithm for ray tracing

► Algoritmo:

4

► Obtener el t inicial, $tMax$.

- La situación más normal es que el origen del rayo no se encuentre en las fronteras de un vóxel, sino dentro de él.
- Sin embargo, los incrementos antes calculados se aplican desde los límites del vóxel.



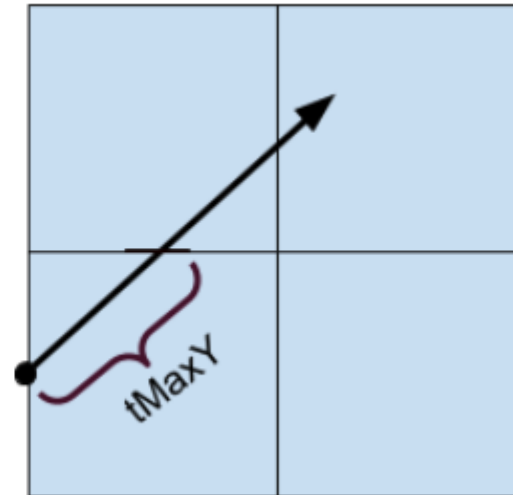
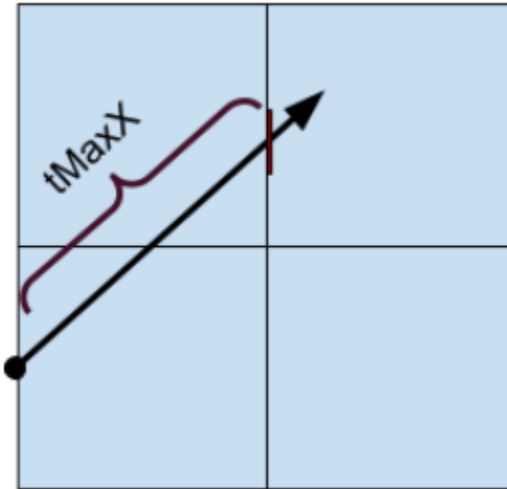
A fast voxel traversal algorithm for ray tracing

► Algoritmo:

4

► Obtener el t inicial, $tMax$.

- El rayo comienza en el vóxel i, j, k .
- Es posible calcular el mínimo punto del vóxel i, j, k : $voxelization.min + voxelSize * indices$
- ¿Cuál es la t ? (Punto obtenido - Origen del rayo) / Dirección del rayo



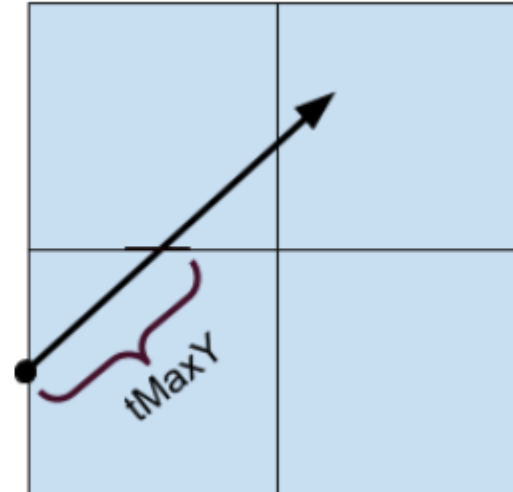
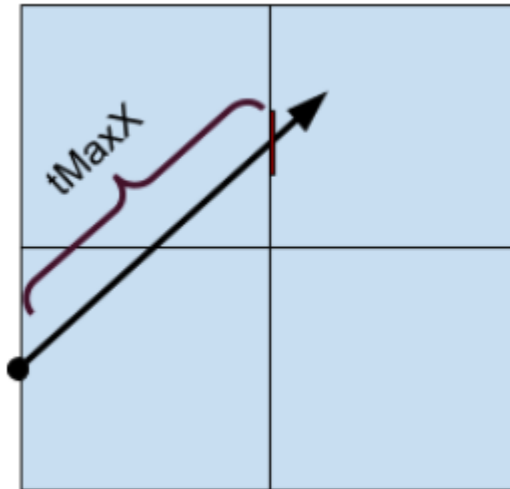
A fast voxel traversal algorithm for ray tracing

► Algoritmo:

4

► Obtener el t inicial, $tMax$.

► Importante: si la dirección del rayo es negativa, se utiliza $i - 1$, $j - 1$, $k - 1$.

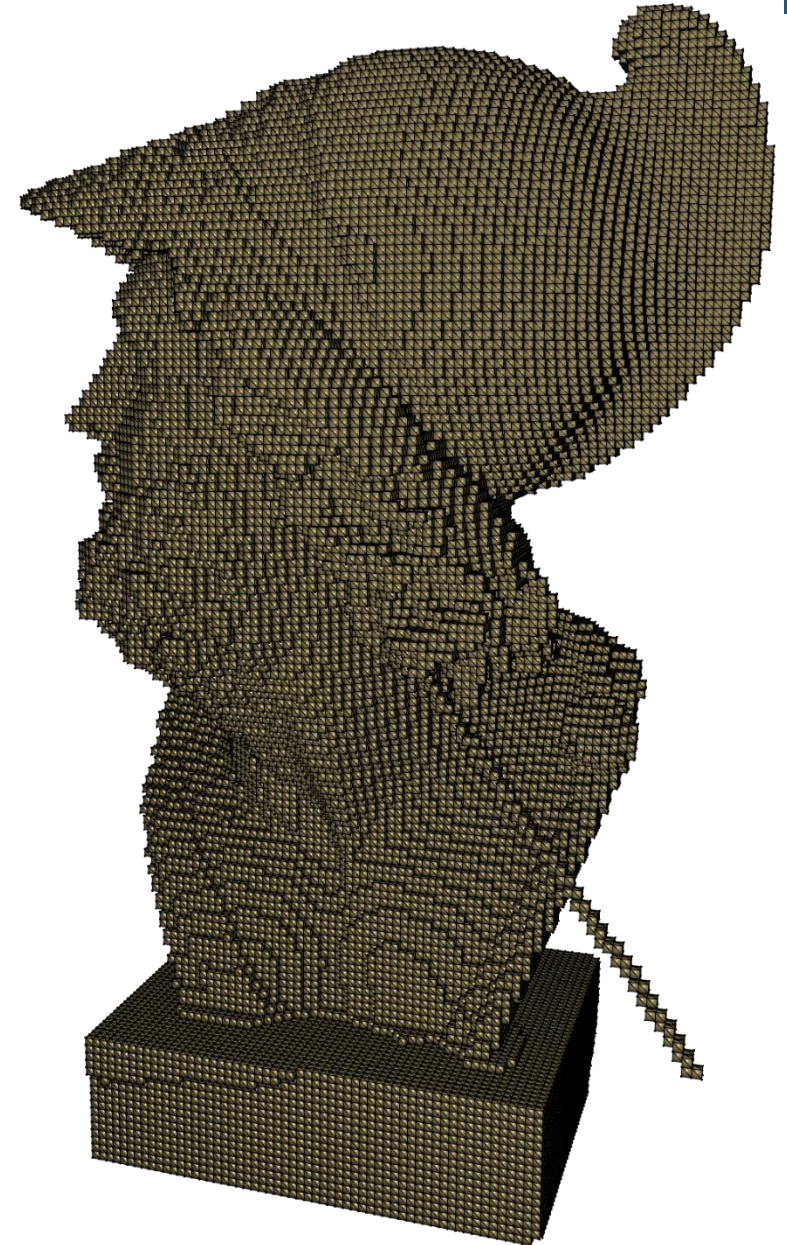


A fast voxel traversal algorithm for ray tracing

32

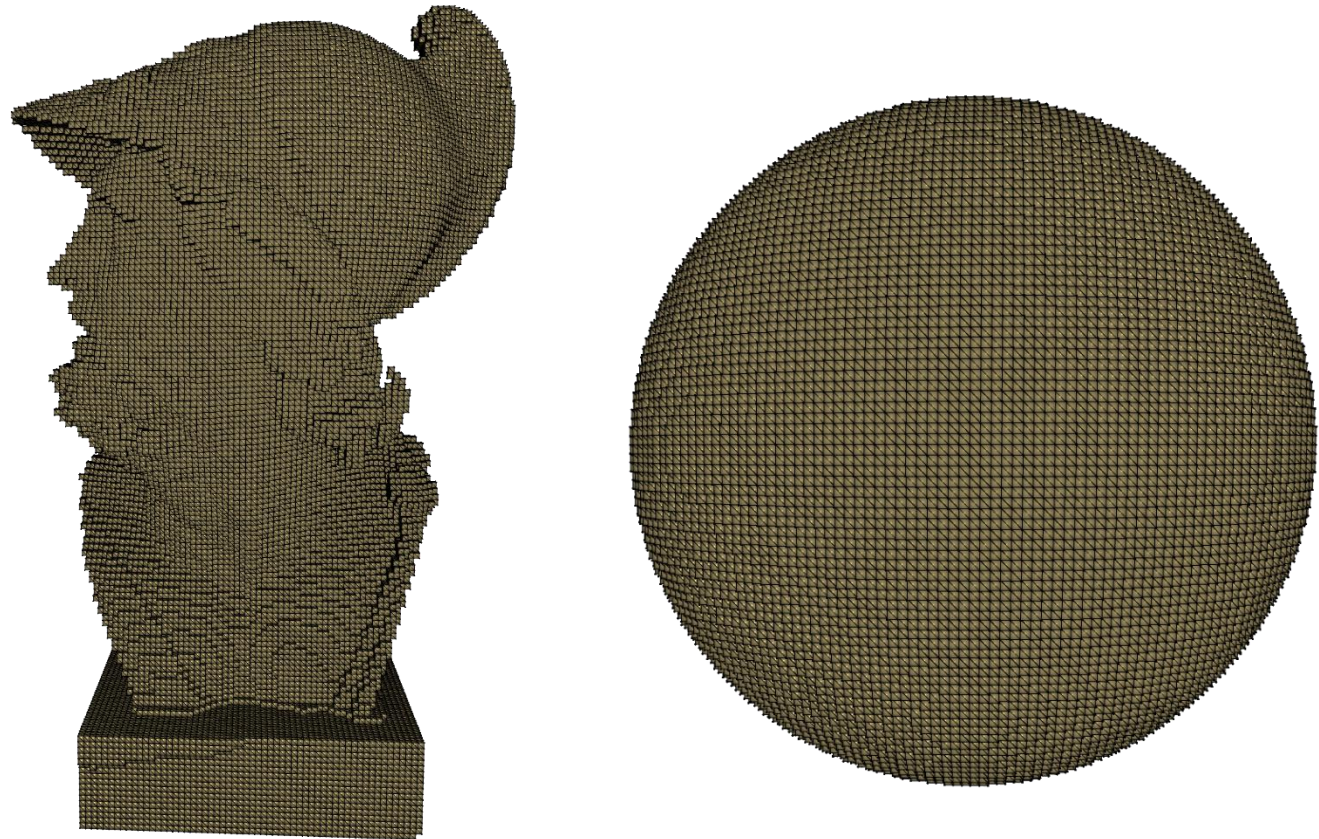
► Algoritmo:

- 5 ► Proceso iterativo.
 - Se recorre la voxelización mientras los índices sean mayores que 0 y menor que el número de subdivisiones.
 - Si $tMaxX < tMaxY$ y $tMaxX < tMaxZ$:
 - $tDeltaX$ se suma a $tMaxX$.
 - $stepX$ se suma a i .

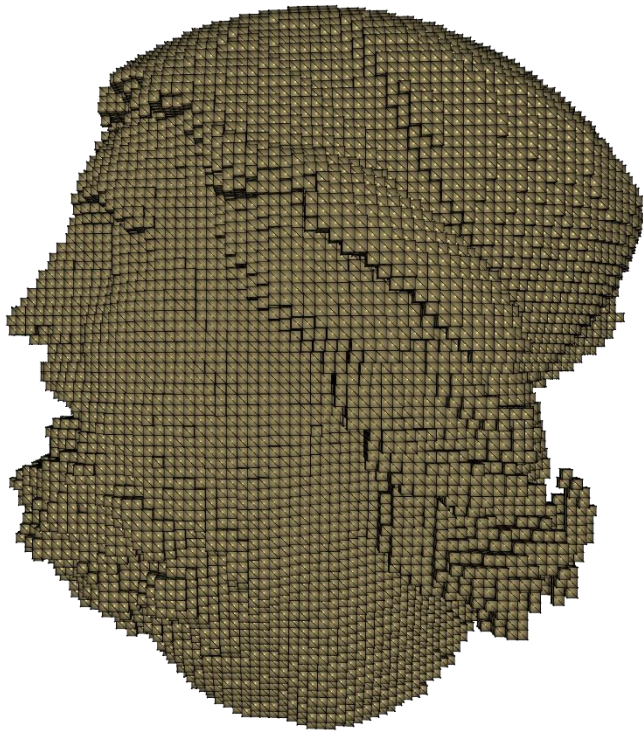


► Dada una voxelización A y una voxelización B:

- Una nueva voxelización que incluye la caja envolvente de A y B, con el tamaño de vóxel de A.



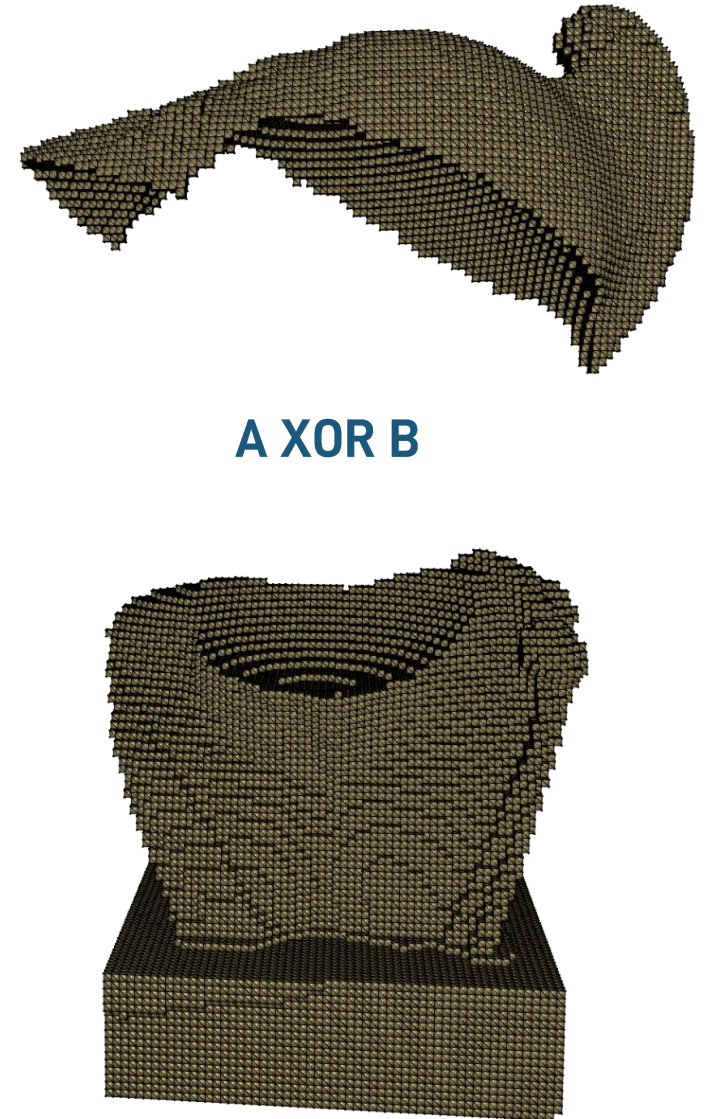
A AND B



A OR B



A XOR B





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Práctica 5.A

Algoritmos geométricos

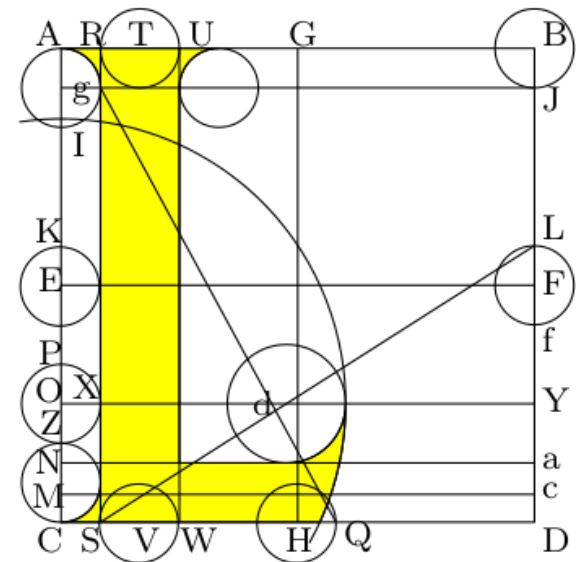
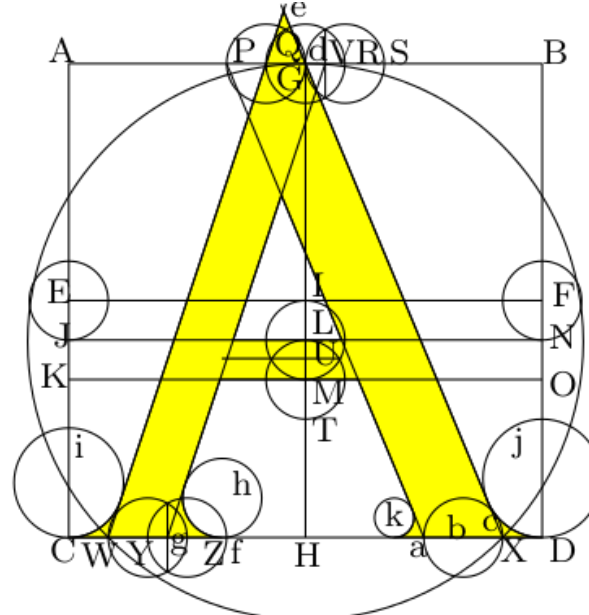
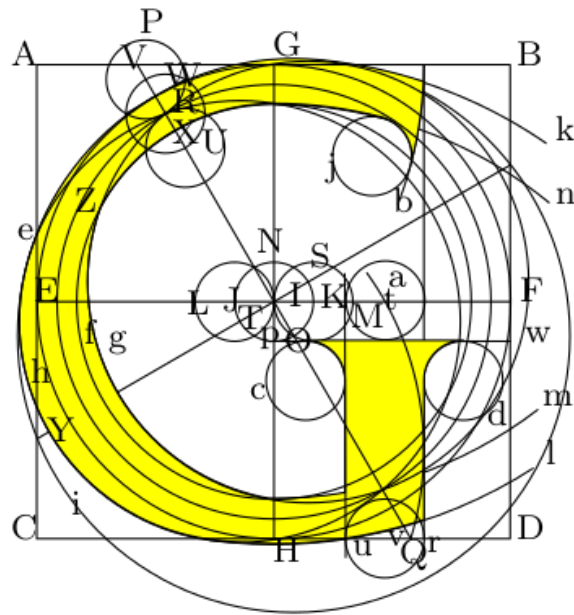
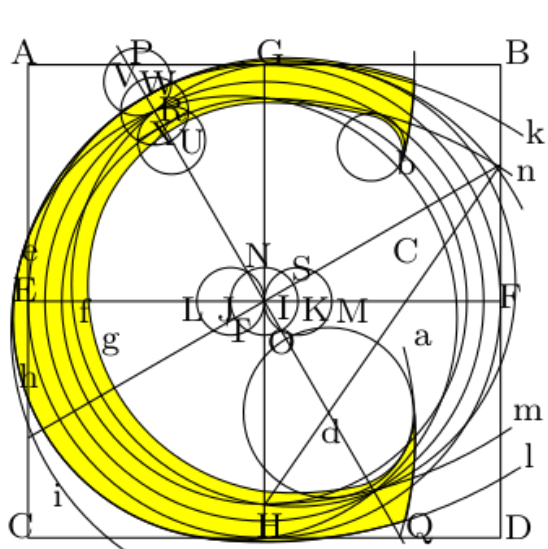
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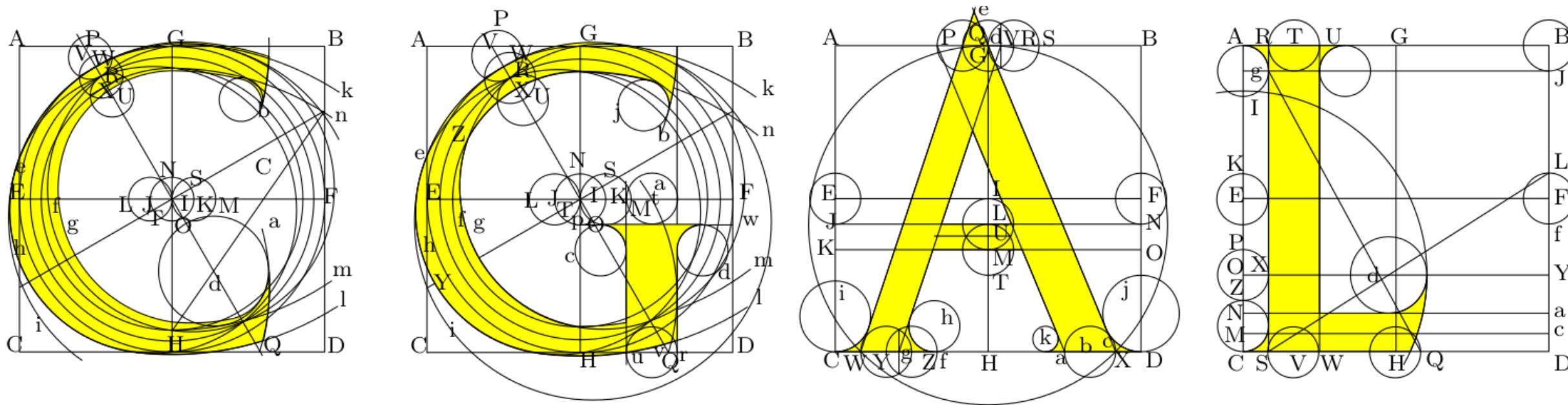
Curso 2022-2023

► The Computational Geometry Algorithms Library

- Procesamiento de nubes de puntos.
- Procesamiento de mallas de triángulos.
- Sintaxis compleja.
 - typedef para simplificarla



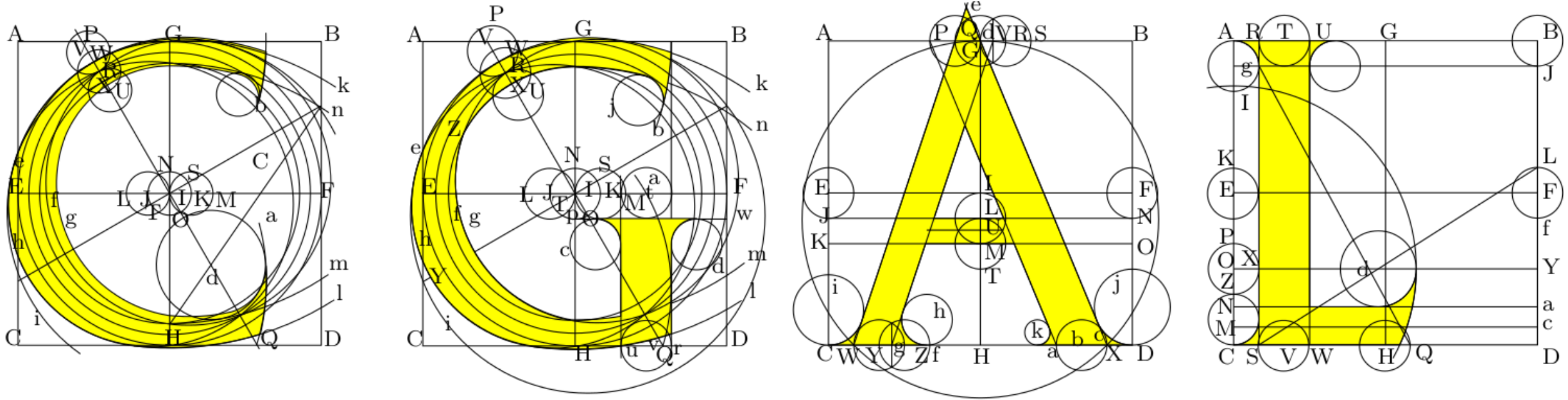
```
► CGAL::Delaunay_triangulation_2<CGAL::Projection_traits_xy_3< CGAL::Exact_predicates_inexact_constructions_kernel>>
```



► The Computational Geometry Algorithms Library

► Sintaxis compleja.

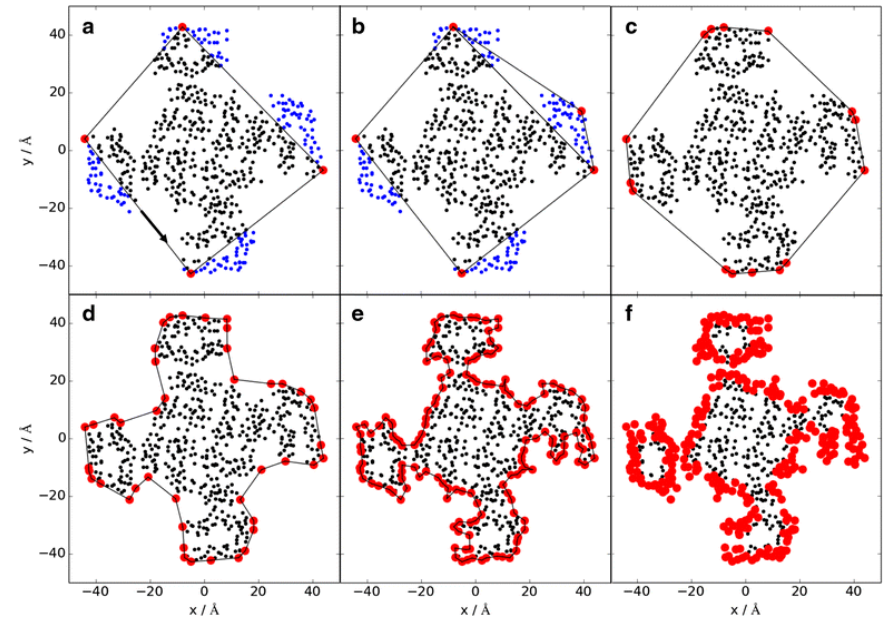
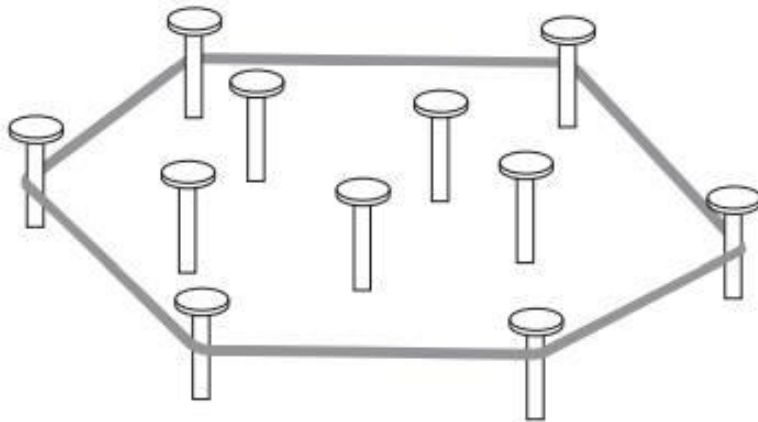
- `typedef CGAL::Exact_predicates_inexact_constructions_kernel K;`
- `typedef CGAL::Projection_traits_xy_3<K> Gt;`
- `typedef CGAL::Delaunay_triangulation_2<Gt> Delaunay;`
- `typedef K::Point_3 Point;`



Envolvente convexa

► La envolvente convexa encapsula un conjunto de puntos.

- Obtiene un envoltorio en forma de malla de triángulos (3D).
- La envolvente convexa es mucho más estricta que la cóncava.
 - Se adapta peor a la forma de los puntos.
 - Aporta una representación mucho más fácil en la que se pueden llevar a cabo comprobaciones con menor tiempo de respuesta.



► Ejemplo de uso de CGAL

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Projection_traits_xy_3.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <fstream>

typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Projection_traits_xy_3<K> Gt;
typedef CGAL::Delaunay_triangulation_2<Gt> Delaunay;
typedef K::Point_3 Point;

int main()
{
    std::ifstream in("data/terrain.cin");
    std::istream_iterator<Point> begin(in);
    std::istream_iterator<Point> end;

    Delaunay dt(begin, end);
    std::cout << dt.number_of_vertices() << std::endl;
    return 0;
}
```

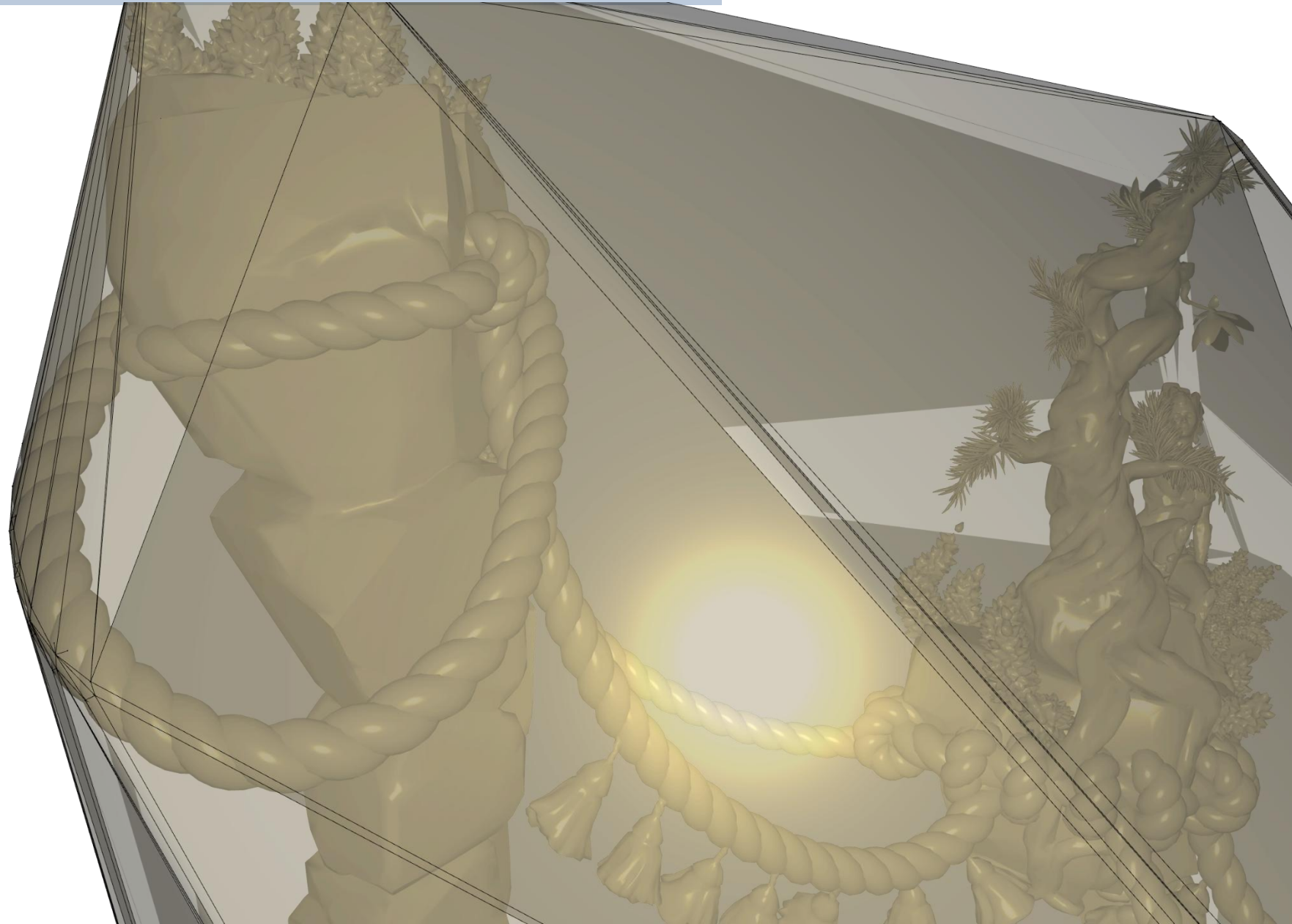
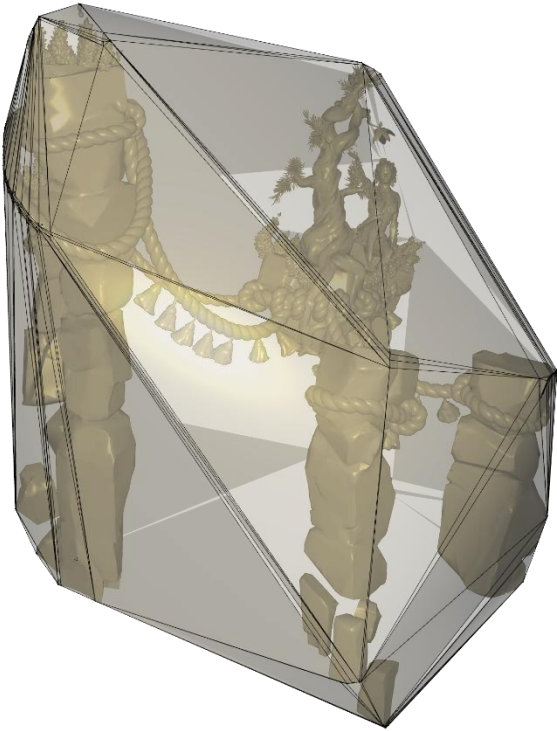
github.com/CGAL/cgal/



Envolvente convexa

► Algoritmo:

1 Convex hull



Envolvente convexa

► Algoritmo:

2 Triangulación con Delaunay + Convexa

